1	Let ABC be a triangle. Let D be the intersection point of the angle bisector
	at A with BC .

Let T be the intersection point of the tangent line to the circumcircle of triangle ABC at point A with the line through B and C.

Let I be the intersection point of the orthogonal line to AT through point D with the altitude h_a of the triangle at point A.

Let P be the midpoint of AB, and let O be the circumcenter of triangle ABC. Let M be the intersection point of AB and TI, and let F be the intersection point of PT and AD.

Prove: MF and AO are orthogonal to each other.

2 Let a, b, c be positive real numbers with a + b + c = 3. Prove that

$$\sqrt{\frac{b}{a^2+3}} + \sqrt{\frac{c}{b^2+3}} + \sqrt{\frac{a}{c^2+3}} \le \frac{3}{2} \sqrt[4]{\frac{1}{abc}}$$

3	Consider a 25 × 25 chessboard with cells $C(i,j)$ for $1 \le i,j \le 25$. Find the
	smallest possible number n of colors with which these cells can be colored
	subject to the following condition: For $1 \le i < j \le 25$ and for $1 \le s < t \le 25$,
	the three cells $C(i, s)$, $C(j, s)$, $C(j, t)$ carry at least two different colors.

(Proposed by Gerhard Woeginger, Austria)

Determine all integers
$$n \ge 1$$
 for which the number $n^8 + n^6 + n^4 + 4$ is prime. (Proposed by Gerhard Woeginger, Austria)