Problem 1	Let ABC be an equilateral triangle, and let P be some point in its circumcircle.
	Determine all positive integers n, for which the value of the sum $S_n(P)$
	$ PA ^n + PB ^n + PC ^n$ is independent of the choice of point P.

Problem 2 Determine the smallest integer n, for which there exist integers x_1, \ldots, x_n and positive integers a_1, \ldots, a_n , so that $x_1 + \cdots + x_n = 0$, $a_1x_1 + \cdots + a_nx_n > 0$ and $a_1^2x_1 + \cdots + a_n^2x_n < 0$.

Problem 3 A set S of integers is Balearic, if there are two (not necessarily distinct) elements $s, s' \in S$ whose sum s+s' is a power of two; otherwise it is called a non-Balearic set. Find an integer n such that $\{1, 2, ..., n\}$ contains a 99-element non-Balearic set, whereas all the 100-element subsets are Balearic.

Problem 4 Let x, y, z and a, b, c be positive real numbers with a + b + c = 1. Prove that

$$\left(x^2 + y^2 + z^2 \right) \left(\frac{a^3}{x^2 + 2y^2} + \frac{b^3}{y^2 + 2z^2} + \frac{c^3}{z^2 + 2x^2} \right) \ \ge \ \frac{1}{9}$$